MANSHALL
1N-37-CR
2605
P15

MODELING OF ROLLING ELEMENT BEARING MECHANICS

CONTRACT NAS 8-38607 MONTHLY TECHNICAL PROGRESS REPORT KHK-10

AEROJET PROPULSION DIVISION P.O. BOX 13222 SACRAMENTO, CALIFORNIA 95813

FEBRUARY 1991

PREPARED BY:

L. M. GREENHILL

PRÍNCIPAL INVESTIGATOR

R. L. BICKFORD

APPROVED BY:

PROGRAM MANAGER

(NASA-CR-188045) MODELING OF ROLLING ELEMENT BEARING MECHANICS Monthly Report, Feb. 1991 (GenCorp Aerojet) 15 p CSCL 131

N91-21530

Unclas 63/37 0002605

I. REPORTING PERIOD OF PERFORMANCE

This report covers the accounting month of February 1991. Beginning with this report, Version 2.0 of the program plan will be used as the schedule and fiscal reference. Further comments relative to this revised plan are given in the following section of this report.

This is month 10 of the 18 month Phase I as given in Version 2.0 of the program plan. With the revision, the overall program extends over 31 months.

Exact reporting period of performance is 01-19-91 to 02-15-91.

The program start date was 05-08-90.

II. PROGRAM STATUS vs. PLAN

PROGRAM PLAN REVISIONS

Beginning with this monthly report, the Version 2.0 program plan presented to the NASA technical monitor, Steve Ryan, on January 15, 1991 will be used to track progress. It is recognized that this replan has not been formally approved by NASA, especially in regards to the accelerated funding required. However, the obsolescence of the original program plan warrants use of this new plan.

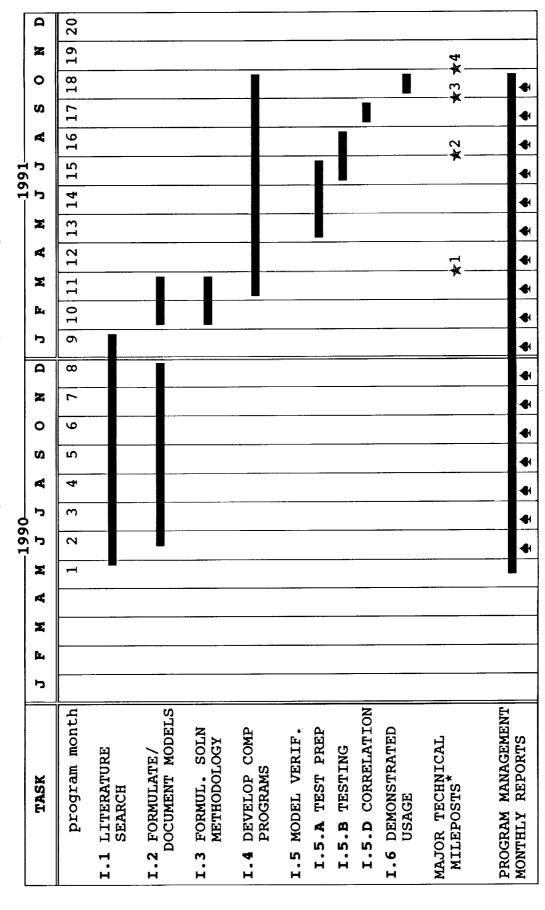
The impact of switching to the Version 2.0 program plan on Phase I activities is minor. Essentially, the duration has been shortened from 19 to 18 months, and some resources have been reallocated.

It is imperative that a decision relevant to adopting the Version 2.0 program plan be made before program month 15 (July 91). At this point, the replan program starts Phase II. If necessary, the program can be stretched to avoid the overlap of development phases, however, an additional replan exercise will be necessary to accommodate this event.

PROGRAM STATUS CHARTS

Program status charts for this month follow on the next three pages. The schedule and funding profiles are for the Version 2.0 program plan. Page 2 contains the Milestone and Schedule Chart. A spreadsheet summary of the program for both salary hours and material (ODC) is given on page 3. Finally, page 4 displays the overall budget versus actuals. Only Phase I data are given, as the other two phases have not started.

VERSION 2.0 PROGRAM PLAN PHASE | MILESTONE SCHEDULE MODELING OF ROLLING ELEMENT BEARING MECHANICS Lyn Greenhill, Principal Investigator Revised 02-07-91



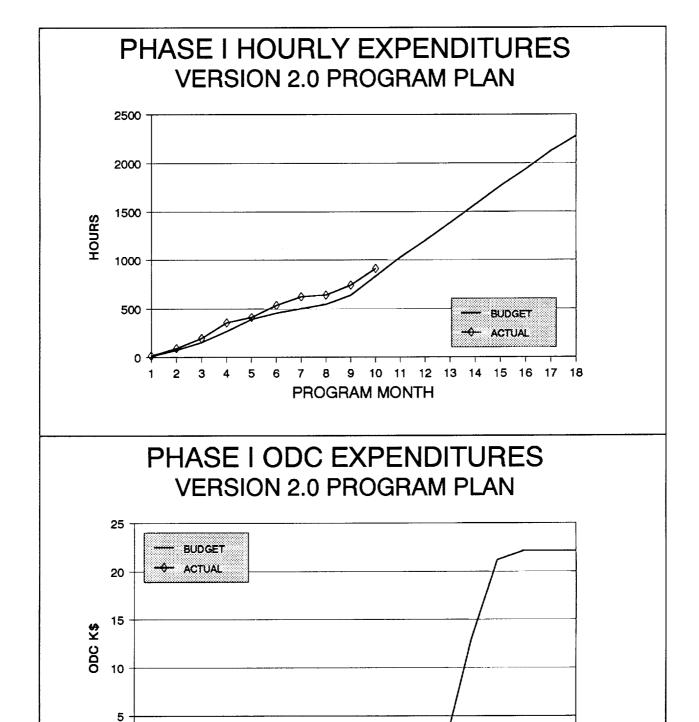
* 1: Theoretical developments complete/doc'd 2: Unverified code complete and documented

3: Testing completed
4: Verified code installed at NASA/MSFC

	_										_									_	_				
	(%)	PROG	c	>	0	*	0		0		0	•	0	(>	_	•	-115		-138	ì	<u> </u>	Š	IOI ALS:	,38 ,38
PLAN	VARIANCES(%)	SCHO	c	>	777	‡	-100		0		0	•	0	(-	_	•	-27		-45	;	<u>‡</u>			-58
	VAR I	COST 8	c	?	u	1	8		0		0	•	0	•	>	_	•	88		8	ĉ	8		LABG E	0
RAN	PCT	O delo	85	38	9 6	2 1	30	0	0	_	0	0	0	0	5	-	67	64	25	Ri	28	3	ļ	# * * *	8
PROGRAM	3	_	7.68 7.68			_	0	0	0	0	0	0	0	0	> 0	-	8	124	2	5 6	42	2		333	911
		18 7						8							ç	b	7	•	9	,	M		155		
1 2.0		17						04						135			7		9		M				
IOI												_		=-									85.		
VERSION		16						3				121					7		v	•	* 1		174	103	2
1		5						8		75	•	41					7	•	9	1	M		<u>8</u>	1741	911
# 10,		14						1 <u>2</u> 0		75							7	•	9	,	~		187	15.7 15.7	911
		13						<u>원</u>		75							7	•	9	1	~		187	1384 1384	911
MONTH		12						3									7		9	1	M		٤ ,		
PROGRAM		=		,	1	120	3	ଯ									7		9	,	~		193		
PRO		9	•	- ç	35	<u> </u>	30		0		0	•	0	(>	c	4	27	9	<u>۰</u> ۱	Μ,	4	193	3 3 3 3 3	911
		Φ;	946	35	? ;	<u>-</u>	0		0		0	•	0	(>	_	4	31	9	<u>ی</u>	M,	-	85	= { = {	743
1991,		ထ	,	4 0	ų c	>	0		0		0	•	0	(>	_	4	•	9	۱-۸	n	>		<u>- 27</u>	
- 1		~	6	35	700	9	0		0		0	•	0	(>	_	4	0	9	ال	ωţ	<u>-</u>		- 38	
EBRUARY	Ξ	9	ψ,	80	0 (75	0		0		0	•	0	(>	_	4	~	9	12	ν,	-	8		
FEB	H MONTH	νį	55	ጸኔ	ţ°	0	0		0		0	•	0	(>	_	4	4	9	٥į	۲	7-		, Second	
	PROGRAM	4	8	\$ †	28	\$	0		0		0	•	0	(>	_	•	۲,	9	2 ;	, 2	٥		35	
NDI	₽	M,	75	34	יי ב		0		0		0	•	0	(>	_	7	15	4	۲,	40	₹		<u> </u>	
K	HOURS	٦į	33	J.	J f	<u>0</u>	0		0		0	•	0	•	>	_	;	7	2		٥;	<u> </u>		35	
MAR	_	_	ď	>	c	>	0		0		0	,	0	•	>	_	× ∞	<u>5</u>	0	0	00	>	ωį	<u> </u>	<u>5</u>
PHASE I LABOR SUMMARY ENDING	TOTAL	HRS	268	774	- 5	180	3	99		162	į	162		135	(k	80	1	8	;	8			227R	į
S S	_					2	; 2 ≥	<u>0</u>	. ¦	5						ei ei							S	Z¥X	
LAE	8		ature	F 6	3 3	Models Form/Doc Soln	Methodology	Dev/Doc Comp	Programs	Pred	}	2		late	•	Demonstrate Heade	Mrds/Tech	ting)	Reporting	we.	Management			
Н	DESCRIPTION		Liter	vearch		Form	F ethor	Dev/D	Progr	Veriticat Test Pren	}	Testi		Correlate	9 20 20	Lemon Lemon	MTGS/	Reporting	Cost	Repor	Progr	aua Manac	BUDGET	ACTUAL	ACT.
ASE	DES		KHK110 Literature	001/07		KHK130		KHK140		MODEL KHK15A		K15B		K150	0,1	KHK 100	KHK400		KHK410		KHK420		MONTHLY		3
PH	¥											I.5.B KHK15B Testing		1.5.D KHK15D			¥		₹		₹		TOTAL MO	¥ ¥	
	TASK		<u> </u>	,	7:	-	:	7.1		Ú.	:	1.5		 	· -	•							5	<u>5</u>	

		_						_		_				_		_			_				
																					i	i,	
PLAN	00C	•	19	107	5	0	c	>	,	0	0		0	(>	è	ţ	-14		0	107.000	ODC 101AL	'n
VERSION 2.0 PROGRAM PLAN	200		929	064 000	10	0	00	>	0	00	00	.0	0	0	٠,	804	2	35	;0	~	1000	CUMULALIVE UNC ICIALS: 1890	1832
0 PJ	ā	2															7	r			40	25.	1832
N 2.	7	:															7	٢			40	7117	832
SIO	7	2					120			100	5						7	r			626	7113 2	832
	ħ	2							8354								7	r			8358	18°	1832
10,	2	<u>t</u>							10920 8								7	r			4 10924 8	826 2	1832
# H	<u> </u>	2							5								7	r			4 0		1832
HONT	5	ī															~	t			40	200 700	
AM 1	-	:															7	•			40	70%	1832
ROGE	Ę	2	0	512	1	0	c	>		0	0	,	0	(3	S;	<u>-</u>	t Mi)	0	804	2 2 2 2 2 3	1832
P.	o		0	_	,	0	•	5		0	0	,	0	•	>	•	><	t -		0	4.	- 8	<u>8</u>
1991	α	•	113	c	•	0	c	>	•	0	0	,	0	•	>	•	> <	†6	2	0	4,0	3 <u>5</u>	1185
RY				885 875 875 875 875 875 875 875 875 875		0	C	>	1	0	0)	0	•	>	•	> <	tur	•	0	404	•	_
BRUA	MONTH	-		3¥	3	0	•	-		0	0		0	•	-	•	- ~		•	2	20.		
FEI	PROGRAM M	30,	8	072	š	0		•		0	0	,	0	,	_ >	,	- ~	, ₇)	0	35.		
ING	BY PRO	ئ 1	0	0 0 4	•	0	•	>		0	0	,	0	(-	N	' ⊃∢	۲ ع		0	56	o 7	164
ENI	\$ 500	16	-	0 k	}	0	c	>		0	0	,	0	(-	N	V ~	t C	,	0	χ;	₹. -	17
KARY	-	-	0	_	•	0	•	>	,	0	0	•	0	•	>	•	>	0	•	0	00	-	0
PHASE I ODC SUMMARY ENDING FEBRUARY 1991, PROGRAM MONTH # 10,	TOTAL	25		780	0		120		19274	Š	8	0		0	i	\$	87	3	0	•		22121	! !
ODC	Z	ture		8.	Form/Doc Soln	Methodology	Dev/Doc Comp	Verification		. ,	2 0	ate		trate		ا	2	2	,	ment		A 44	.
E I	DESCRIPTION	Litera	Search	Form/0	Form/C	Methoc	Dev/Do		Test Prep		lescil	Correlate		Demonstrate	Usage	Mtgs/	Keporting	Reporting	Program	Management		ACTUAL REDGET	
PHAE	DESC	KHK110 Literature		X¥¥129	KHX130		KHK140	Model	¥	7	1,3,6 KMKI36 lesting	1.5.0 KHK150		χ¥160		K400	VUV. 10		KHK420		MONTHLY		E C
	TASK	1.1		1.2	1.3	1	1.4	<i>u</i>	1.5.A	L	ָת מיריים	1.5.0		9.1							TOTAL	10 A	

For each task, the first row are planned allocations, the second row are actuals. Cumulative labor percent completion is a weighted average of all tasks combined. ODC plan values do not include material burden. **−**.ν.ν. NOTES:



PROGRAM MONTH

10 11 12

5

13 14 15 16 17

EXPLANATIONS OF SIGNIFICANT VARIANCES AND CORRECTIVE ACTION

Program Variances:

KHK120: A computer charge of \$512 was made on this task during February. The code that

was used (MACSYMA) is only available on the VAX network, necessitating the

expenditure, although the amount was surprising.

ACTION: This expenditure will be covered with other ODC funds. No further use of the code

will be authorized.

KHK400: Replan activities associated with contract requirements resulted in 27 hours being

spent.

ACTION: It appears that with the replan effort, this activity may be underfunded. It will be

monitored over the course of the next few months to determine if the initial estimates are adequate and what additional allocation will be needed to balance

expenditures with budget.

II. TECHNICAL PROGRESS

Work Package KHK110 (Literature Search)

We have obtained the remaining documentation on computer codes RAPIDREB and SHABERTH, thus concluding this task. A complete list of references for the quasi-static solution are given in the Appendix.

Work Package KHK120 (Formulate/Document Models)

The classical bearing mechanics work of Jones [1]* and Harris [2] were studied in detail, primarily with reference to angular contact ball bearings. All of the equations related to bearing geometry, relative motions of rolling elements, and internal rolling-element load distribution were rederived to determine implicit assumptions in the formulations. These derivations were facilitated by using the symbolic analysis code MACSYMA.

A preliminary assessment of some of the assumptions inherent in traditional bearing mechanics, relative to structural flexibility analysis, is as follows:

- 1. Except for Hertzian contact between the balls and races, all the bearing components (inner ring, outer ring and housing) are considered rigid. Elastic displacements of these components, as well as local deformations of a hollow shaft, could significantly change the quasi-static load distribution between the components.
- 2. The azimuth angle defining ball location (ψ_j) is considered constant, and the rigid-body small displacements of the inner ring are described by only five degrees of freedom (DOF). With general elastic deformations of the bearing components, small displacements could occur in the tangential (azimuth) direction, and the rigid-body small displacements of the inner ring could require a sixth DOF at the shaft/inner ring interface (i. e., ψ_i not constant).
- 3. Some contributions to inner ring rigid-body motion, which may be of the same order as elastic deflections, are neglected. These contributions become evident when the coordinate system fixed at the shaft center line is allowed to move with the shaft relative to inertial space. The use of the moving coordinate system will facilitate the proposed study of enforced motion in Phase II.
- 4. The initial radial distance from the shaft center to the inner race curvature center (R_i) is used as a constant to calculate the forces and moments at the bearing center for comparison with the known applied forces and moments. The actual coordinates from the ball/inner race contact points to the fixed point of force and moment application should properly be used.
- 5. The inner race and outer race curvature centers necessarily move with their respective races as part of a rigid body. These curvature centers, required to determine normal force directions at the ball/race contact points, must be considered part of the flexible inner and outer rings for the subsequent quasi-static analysis.

Numbers in brackets denote references given in Section IV of the report

- 6. Traction forces applied to the ball by relative fluid motion are neglected. Only the friction forces needed to react the gyroscopic moment are included in the force equilibrium equations.
- 7. The concept of race-ball control utilized by Jones [1], in which spin occurs only at the outer race or at the inner race, is not supported by subsequent work such as Harris [2] and Walters [3]. According to these sources, inner-race control is impossible but outer-race control can be approximated in certain situations. Usually ball spin occurs at both races. We will formulate the bearing mechanics equations without reliance on this assumption.

At the time these traditional formulations were developed, such assumptions were probably necessary to obtain a timely solution with the computational power available. The figure on page 8, taken from Harris [2] page 256, can be used to illustrate some of these common assumptions in the kinematic analysis of ball bearings.

In the unloaded condition, the initial position of the inner and outer raceway groove curvature centers and the ball center are collinear (and coplanar), separated by the distance BD. In terms of the inner and outer raceway curvatures $(f_i \text{ and } f_o)$, BD may be expressed as:

$$BD = (f_0 + f_i - 1)D (1)$$

where D is the ball diameter. This dimension implies that the internal clearance in the bearing has been absorbed by axial translation of the inner race.

Assuming a fixed outer raceway groove curvature center, the application of static load and centrifugal force results in radial and axial (but not tangential) motion of the *inner* raceway groove curvature center, denoted by quantities Δr and Δz . In terms of the unknown rigid body relative radial, axial, and angular displacements of the inner and outer rings, the motion is expressed as:

$$\Delta r = \delta_r \cos \psi_j$$

$$\Delta z = \delta_a + \theta R_i \cos \psi_j$$
(2)

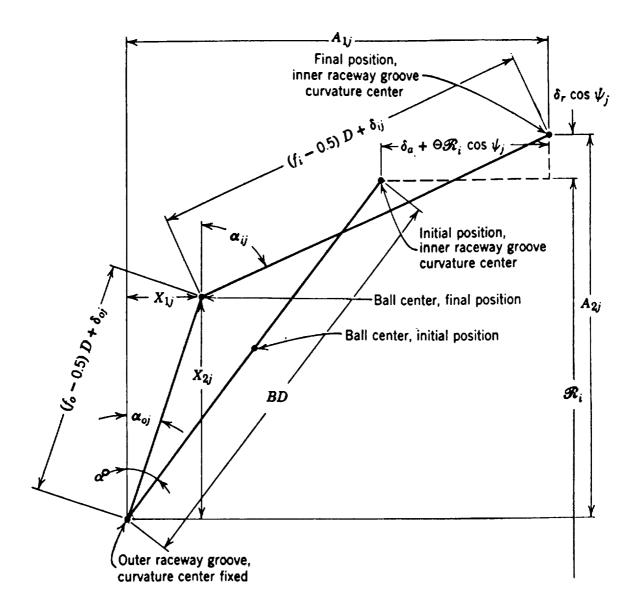
The figure illustrates the key dimension R_{ij} the initial radius of the inner raceway groove curvature center, which is used as a *constant* in the Jones and Harris force analyses. Note that the figure and these equations express the relative motion of the inner and outer rings in terms of three degrees of freedom. In actuality, both Jones and Harris utilize five degrees of freedom in their complete analysis, resolving the motion into a Cartesian coordinate system with only the angular position in the axial direction fixed (again, no tangential motion allowed).

Using the deflections due to load and speed given in equation (2), coupled with the unloaded dimension BD from (1), the relative axial and radial motion of the loci of inner and outer raceway groove curvature centers at any ball position is:

$$A_{1j} = BD \sin \alpha^{0} + \Delta z$$

$$A_{2j} = BD \cos \alpha^{0} + \Delta r$$
(3)

where α^0 is the initial contact angle. Since the external forces and/or displacements exerted on the inner race are known, and the internal forces generated by the ball rotation (centrifugal and gyroscopic) can be calculated, the solution to equation (3) yields the full specification of the displacement in the traditional bearing mechanics analysis.



In order to obtain the relative curvature center displacements, the kinematic equations expressed by (3) were reformulated by Jones and Harris for the ball center displacements X_{Ij} and X_{2j} and inner and outer ring contact angles α_{ij} and α_{oj} and solved using a Newton-Raphson iteration. Actually, the contact angles are not obtained directly, the iterative solution obtains values for X_{Ij} , X_{2j} , δ_{ij} , and δ_{oj} , where the latter two quantities are the inner and outer ring contact deformations. These hertzian deflections are the only flexibility in the analysis. As was discussed in the work of Davis and Vallance [4], this limited compliance can result in significant differences in contact angle and ball load distributions compared to a fully flexible ring analysis.

Once these four terms are obtained, forces and moments satisfying static equilibrium can be computed, although both Jones and Harris use R_i as the moment arm. This means that the moments exerted by the inner ring on the shaft use a lever arm foreshortened by the Δr displacement. The static equilibrium forces are combined with the solution for X_{Ij} , X_{2j} , δ_{ij} , and δ_{oj} to calculate the primary unknown relative displacements δ_r , δ_{ar} and θ using iterative refinement.

The Newton-Raphson iteration scheme used by Jones and Harris requires numerous partial derivatives of some rather complicated expressions. If our analysis indicates that these terms must be rederived, we found that the use of MACSYMA can significantly reduce the time and labor required to obtain such quantities.

Work Package KHK130 (Formulate/Document Solution Methodology)

We had intended to begin work on this task by examining the codes we have obtained. This effort was deferred until we could adequately review the documentation obtained on the two primary bearing mechanics programs, RAPIDREB and SHABERTH, which we received this month.

Work Package KHK400 (Meetings/Technical Reporting)

The Version 2.0 program plan was formally submitted through contractual channels for approval by NASA. D'Jack Klingler (Aerojet) sent Joyce Mallory (NASA) two memos, one describing the revised program plan, and the other documenting a phone call in regard to personnel changes.

Work Package KHK410 (Cost Reporting)

Monthly report and support of replan activities.

Work Package KHK420 (Program Management)

Support of replan activity.

III. WORK FOR NEXT REPORTING PERIOD

Work Package KHK120 (Formulate/Document Models)

We will conclude work on the study of the theoretical aspects of ball and roller bearing kinematics and dynamics as well as the development of theory to support the incorporation of race flexibility into bearing mechanics software.

Work Package KHK130 (Formulate/Document Solution Methodology)

We will review the theoretical manuals obtained for the primary bearing mechanics analysis codes, RAPIDREB and SHABERTH, primarily to determine the applicability of the codes to support the incorporation of flexibility, enforced motion, and transient analyses. Where possible, we will compare the quasi-static solution approach in the codes to the methodology we have developed, in order to determine the amount of modification required.

Work Package KHK400 (Meetings/Technical Reporting)

Monthly report activity.

Work Package KHK410 (Cost Reporting)

Monthly report activity.

Work Package KHK420 (Program Management)

Monthly report activity.

IV. REFERENCES

- 1. Jones, A. B., "A General Theory for Elastically Constrained Ball and Radial Roller Bearings Under Arbitrary Load and Speed Conditions", *Jrnl Basic Engr, ASME Trans*, Vol 82, pp 309-320, 1960.
- 2. Harris, T. A., Rolling Bearing Analysis, 2nd Edition, John Wiley, 1984.
- 3. Walters, C. T., "The Dynamics of Ball Bearings", *Jrnl Lubrication Technology*, *ASME Trans*, Vol 93, pp 1-10, 1971.
- 4. Davis, R. R., and Vallance, C. S., "Incorporating General Race and Housing Flexibility and Deadband in Rolling Element Bearing Analysis", Rotordynamic Instability Problems in High-Performance Turbomachinery 1988, NASA CP 3026, May 1988.

Appendix A

List of Quasi-Static Analysis Technical References

- Crecelius, W. J., and Pirvics, J., Computer Program Operation Manual on SHABERTH, A Computer Program for the Analysis of the Steady-State and Transient Thermal Performance of Shaft Bearing Systems, USAF Technical Report AFAPL-TR-76-90, U. S. Aero Propulsion Lab, Wright Paterson AFB, 1976.
- Filetti, E. G. and Rumbarger, J. H., "A General Method for Predicting the Influence of Structural Support Upon Rolling Element Bearing Performance", *Jrnl Lubrication Technology, ASME Trans*, Vol 92, pp 121-128, 1970.
- Gupta, P. K., "A Review of Computerized Simulations of Roller Bearing Performance", Computer-Aided Design of Bearings and Seals, Proc. AMSE Annual Meeting, pp 19-30, Dec 1976.
- Gupta, P. K., Interactive Graphic Simulation of Rolling Element Bearings Phase I: Low Frequency Phenomenon and RAPIDREB Development, USAF Technical Report AFWAL-TR-81-4148, U. S. Aero Propulsion Lab, Wright Paterson AFB, 1981.
- Hadden, G. B., Kleckner, R. J., Ragen, M. A., and Sheynin, L., Steady State and Transient Thermal Analysis of a Shaft Bearing System Including Ball, Cylindrical, and Tapered Roller Bearings (SHABERTH User's Manual), NASA Technical CR 165365, NASA/Lewis, 1981.
- Harris, T. A. and Mindel, M. H., "Rolling Element Bearing Dynamics", Wear, Vol 23, pp 311-337, 1973.
- Jones, A. B., "A General Theory for Elastically Constrained Ball and Radial Roller Bearings Under Arbitrary Load and Speed Conditions", *Jrnl Basic Engr, ASME Trans*, Vol 82, pp 309-320, 1960.
- Jones, A. B., "The Mathematical Theory of Rolling-Element Bearings", Mechanical Design and Systems Handbook, Chapter 13, Rothbart, Ed., McGraw-Hill, 1963.
- Kleckner, R. J., Pirvics, J. and Castelli, V., "High-Speed Cylindrical Rolling Element Bearing Analysis CYBEAN Analytical Formulation", *Jrnl Lubrication Technology*, *ASME Trans*, Vol 102, pp 380-390, 1980.
- Kleckner, R. J. and Pirvics, J., "High-Speed Cylindrical Rolling Element Bearing Analysis Computer Program CYBEAN Volumes I and II", NASA CR 159460, NASA Lewis Research Center, 1978.
- Kleckner, R. J. and Pirvics, J., "Spherical Roller Bearing Analysis", *Jrnl Lubrication Technology*, ASME Trans, Vol 104, pp 99-108, 1982.
- Kleckner, R. J. and Pirvics, J., "Spherical Roller Bearing Analysis Computer Program SPHERBEAN Volumes I, II, and III", NASA CR 165203, NASA Lewis Research Center, 1980.
- de Mul, J. M., Vree, J. M., and Maas, D. A., "Equilibrium and Associated Load Distribution in Ball and Roller Bearings Loaded in Five Degrees of Freedom While Neglecting Friction Part I: General Theory and Application to Ball Bearings", ASME Paper 88-Trib-9.

Appendix A

List of Quasi-Static Analysis Technical References

de Mul, J. M., Vree, J. M., and Maas, D. A., "Equilibrium and Associated Load Distribution in Ball and Roller Bearings Loaded in Five Degrees of Freedom While Neglecting Friction - Part II: Application to Roller Bearings and Experimental Verification", ASME Paper 88-Trib-10.

Rumbarger, J. H., Filetti, E. G., and Gubernick, D., "Gas Turbine Engine Mainshaft Roller Bearing-System Analysis", *Jrnl Lubrication Technology, ASME Trans*, Vol 95, pp 401-416, 1973.

Sibley, L. B. and Pirvics, J., "Computer Analysis of Roller Bearings", Computer-Aided Design of Bearings and Seals, Proc. AMSE Annual Meeting, pp 95-115, Dec 1976.

Walters, C. T., "The Dynamics of Ball Bearings", *Jrnl Lubrication Technology, ASME Trans*, Vol 93, pp 1-10, 1971.

Netional Aeronautics and Space Administration	Report Docu	mentation Pag	Page						
1. Report No.	2. Government Acces	sion No.	3. Recipient's Catal	og No.					
4. Title and Subtitle	<u> </u>		5. Report Date						
Modeling of Rolling Elemen	nt Bearing Mechan	ics	February 19	ary 1991					
	J		6. Performing Organ	nization Code					
7. Author(s)		8. Performing Organization Report No							
L. M. Greenhill		KHK-10							
9. Performing Organization Name and Addre		11. Contract or Grant No.							
Aerojet Propulsion Division P. O. Box 13222			NAS 8-386	07					
Sacramento, California 958	13-6000	-		t and Period Covered					
12. Sponsoring Agency Name and Address			Monthly Pro	ogress Report 0/91 to 02/15/91					
National Aeronautics and Sp		n -	14. Sponsoring Age						
George C. Marshall Space F Marshall Space Flight Cente			•						
15. Supplementary Notes									
This monthly technical pro February 1991, Program month 2	ogress report desc 10 of 31, Phase I m	cribes the work p nonth 10 of 18 (Ve	erformed in acrain acrain 2.0 Progra	ecounting month am Plan).					
The NASA technical monito	or is S. Ryan, MSF	C/ED14.							
16. Abstract			·						
Rolling element bearings protating components in the hig (SSME). Knowledge of bearing essential to predicting and under stability, critical speeds, and be models and computer programs bearings under the loading and performance rocket engines. relationships, stiffness and dam stability.	h performance tung behavior under standing the overa caring life. The out to describe the renvironmental cor This includes ping, rolling elem	rbomachinery of to various loading a ll behavior of turbo bjective of this we nechanical behavior encountered characteristics sugart loads for life	he Space Shuttend environment opumps, includitions is to developed or of ball and ded in the SSME and the prediction, and	tal conditions is ng rotordynamic op mathematical cylindrical roller and future high ear load/motion roller and cage					
The work is divided into th Loading and Dissipative Force emphasizes inclusion of race ar techniques.	Analysis, and I	II: Constrained I	Dynamic Analy	rsis. The work					
17. Key Words (Suggested by Author(s))		18. Distribution Stateme	ent						
Rolling Element, Bearings, Finite Element, Stability, Mechanics, Clearance, InterDeadband, Stiffness, Dampi	nal Loads,	Unclassified	- Unlimited						
19. Security Classif. (of this report)	20. Security Classif. (c	f this page)	21. No. of pages	22. Price					

Unclassified

13

Unclassified